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Mathematical Topics Between Classical and Quantum Mechanics

With 15 Illustrations



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I realize that the disappearance of a culture does not signify the disappearance of human value, but simply of certain means of expressing this value, yet the fact remains that I have no sympathy for the current of European civilization and do not understand its goals, if it has any. So I am really writing for friends who are scattered throughout the corners of the globe.

Our civilization is characterized by the word "progress". Progress is its form rather than making progress one of its features. Typically it constructs. It is occupied with building an ever more complicated structure. And even clarity is only sought as a means to this end, not as an end in itself. For me on the contrary clarity, perspicuity are valuable in themselves. I am not interested in constructing a building, so much as in having a perspicuous view of the foundations of typical buildings.

Ludwig Wittgenstein

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The book was written during a happy time, shared with Imke and our cat Pauli.

Klaas Landsman
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